Partial Quotients Question: 550 ÷ 15			
Sample Solutions:			
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
Multiplying Up			
<u>Question:</u> 550 ÷ 15			
Sample Solution:			
$15 \times 10 = 150$ 15 × 10 = 150 450	15 x 20 = 300	$15 \times 30 = 450$	
$15 \times 10 = 150$ 150	15×10^{-130} $15 \times 5 = 75$	$15 \times 36 = 540$	
15 x 2 = 30] 480	$15 \times 1 = 15$ $15 \times 36 = 540$	550 ÷ 15 = 36 r 10	
15 x 2 = 30] 510	550 ÷ 15 = 36 r 10		
15 x 2 = 30] 540			
15 x 36 = 540 + 10			
550 ÷ 15 = 36 r 10			

<u>Division</u>

These strategies should be discovered, explored, and modeled by the students

Multiplication

Making Landmark or Friendly Numbers	Partial Products		
Question: 9 x 29	<u>Question:</u> 4 x 115		
Sample Solutions:	Sample Solution:		
9 x 30 = 270 "that's one group of 9 too much, so" 270 - 9 = 261 Or 9 x 25 = 225 "because 8 25's is 200, so 1 more 25 is 225" 9 x 2 = 18 9 x 2 = 18 and 18 + 18 = 36. 225 + 36 = 261	$4 \times 115 = 4 \times 100 + 4 \times 10 + 4 \times 5$ $4 \times 100 = 400$ $4 \times 10 = 40$ $4 \times 5 = 20$ $400 + 40 + 20 = 460$ $100 10 5$ $4 4 \times 100 = 400 4 \times 10 = 40 4 \times 5 = 20$		
Doubling and Halving	Breaking Factors into Smaller Factors		
Question: 8 x 6	Question: 8 x 25		
Sample Solution: Doubling and Halving can help students relate facts that they are unsure of to facts with which they are fluent. Image: Constraint of the section to the section to the top right to make a 4 x 12 array. I know that's 48 because 4 x 10 = 40 and 4 x 2 = 8. 40 + 8 = 48 Image: Constraint of the section to the top right to make a 4 x 10 = 40 and 4 x 2 = 8. 40 + 8 = 48	Sample Solution: $8 = 2 \times 4$ $25 \times 4 = 100$ $100 \times 2 = 200$, so $8 \times 25 = 200$ 25 4 4 $\times 25 = 100$ 4 4 $\times 25 = 100$		

These strategies should be discovered, explored, and modeled by the students